

DESIGN AND ANALYSIS OF ACCELERATED LIFE TESTING AND IT'S APPLICATION UNDER REBATE WARRANTY

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ABSTRACT

At the point when a thing was demonstrated to be liberated from blemishes or repeating disappointments when it left the maker, quality targets were accepted to have been met until the last part of the 1960s. The study deals with the advancement of accelerated life testing in the field of product warranty. The expected total cost and expected cost rate for age replacement is estimated under warranty policy using Accelerated Life Testing (ALT) plans. Under constant stress, the lifetimes of the units are assumed to follow generalised exponential distribution. The estimation process is carried through maximum likelihood estimation method. Also, the Age Replacement Policy under Pro-rate Rebate Warranty is discussed. Finally, an application example is presented to illustrate the theoretical results.

Key words : *Accelerated Life Testing, Rebate Warranty*

INTRODUCTION

Each creator of merchandise these days needs to support deals by offering motivating forces to clients looking like guarantees and certifications. It is a proper commitment made by makers to clients that, inside a given time span, they will, at their choice, fix or supplant the merchandise they bought. Moreover, it fills in as a method for advancing the item's quality and increment deals. Different times, a regulative cycle commands that makers offer a guarantee with an end goal to shield the public interest. (Blischke and Murthy, 1992a, 1992b, 1994; Chien, 2010) give a careful investigation of various issues connecting with item guarantees.

One of the most well known assortments of guarantee inclusion is a discount guarantee. On the off chance that an item glitches inside the guarantee period, the maker (dealer) will repay the client (purchaser) for a piece of the price tag. Batteries and tires are two normal instances of merchandise presented under discount plans. The maker is expected to give free support of the item during the guarantee time frame under a disappointment free guarantee, one more well known sort of guarantee strategy. Family hardware and gadgets might be advertised under disappointment free assurances. Supportive of rata discounts and single amount refunds are the two most predominant varieties of refund arrangements. The two kinds of disappointment free strategies are commonly recharging and non-restoring. You can find extra examination on guarantee strategies and conversations connected to them in Murthy (1990), Mitra and Patankar (1993), and Murthy and Blischke (1992).

Makers may possibly offer impetuses assuming they trust their items and accept they will be valuable for essentially the term of the expressed guarantee. Subsequently, testing the things' steadfastness and execution prior to delivering them onto the market is pivotal for makers. To expect an item's life expectancy under normal use settings, sped up life testing includes exposing the item to higher stressors than expected. Producers can estimate different consumptions connected with the merchandise under guarantee by utilizing sped up life testing. The extended life expectancy of the present items, the speedy circle back among plan and delivery, and the trouble of testing items that are constantly utilized under ordinary conditions are the critical drivers behind sped up life testing. To offer ideal data with respect to the existence dissemination of things, sped up life testing is utilized. Moreover, scientists mixed guarantees models, for example, For an item populace that would experience different feelings of anxiety, Guangbin Yang (2010) proposed a technique for estimating the guarantee cost and its certainty

span utilizing sped up life tests did in the beginning phases of the item life cycle. El-Dessoukey (2015) utilized Exponentiated Pareto conveyance and Sped up Life Tests for age-substitution arrangements under guarantee. This part clarifies how for gauge the expense old enough substitution of units or things covered by guarantee strategy utilizing sped up life testing techniques. The life expectancy of units are accepted to follow a summed up dramatic circulation under steady pressure. Moreover, it characterized the supportive of rata refund guarantee's age substitution strategy for non-repairable hardware.

MODEL DESCRIPTION AND TEST METHOD

Using information assembled under sped up conditions, sped up life testing (ALT) is a habitually involved strategy for anticipating the reliability of frameworks or parts under typical working circumstances. It is commonly done utilizing one of two strategies. The first is called sped up disappointment time (ALT), and it alludes to testing an item or part under typical circumstances yet with expanded force. This technique is fitting for items or parts that are utilized ceaselessly, like toaster ovens, lights, warmers, and tires. The second sort of sped up pressure includes utilizing an item or part at an anxiety that is higher than expected to direct ALT. We should discover the accompanying while making an ALT plan: I. The measurable appropriation of item disappointment rates.

- The sort of information utilized, whether thorough or blue-penciled.
- The editing strategy.
- Such pressure that will be applied during the examination.
- The degree of stress for each chosen pressure type.
- The number of test units ought to be relegated to each anxiety.

The numerical model depicting the connection among stress and life (the life-stress relationship) is thing number seven.

Under the assumption that the unit lifetimes follow a summed up outstanding dispersion, this study utilizes consistent pressure and type-I edited information. K degrees of high anxieties exist. Assume that V_j , $j = 1, 2, \dots, K$ and that V_{i1} is the normal use condition meeting V_j V_1 V_2 V_k . At the point when the examination arrives at the noticed number of disappointments among thesenj units at each feeling of anxiety, the investigation is finished. Allude to Abdel-Ghaly et al. (1998), El-Dessouky (2001), Attia et al. (2011), and Attia et al. (2013) for a careful survey of consistent pressure ALT.

While concentrating on a few life expectancy informational collections, it has been found that the two-boundary Summed up Remarkable conveyance can be utilized rather prudently, particularly in replacement of the two-boundary gamma and two-boundary Weibull dispersions (see Gupta and Kundu1999). It can have expanding or diminishing disappointment rates relying upon the structure boundary. Given by is a summed up outstanding circulation's likelihood thickness capability (pdf).

$$f(t_{ij}, \alpha_j, \beta) = \frac{\alpha_j}{\beta} e^{-\frac{t_{ij}}{\beta}} \left(1 - e^{-\frac{t_{ij}}{\beta}}\right)^{\alpha_j - 1}; \alpha_j > 0, \beta > 0, t_{ij} > 0$$

where the circulation's scale boundary is 0 and its shape boundary is j . $GE(\cdot, \cdot)$ will represent the GE circulation with the shape boundary and the scale boundary. The remarkable dissemination with the scale boundary is addressed as $GE(1, \cdot)$. The summed up dramatic appropriation's (GED) combined dissemination capability (CDF) is

$$F(t_{ij}, \alpha_j, \lambda) = \left(1 - e^{-\frac{t_{ij}}{\beta}}\right)^{\alpha_j}; \alpha_j > 0, \beta > 0, t_{ij} > 0$$

The Generalised Exponential distribution's survival function has the following shape.

$$S(t_{ij}, \alpha_j, \lambda) = 1 - \left(1 - e^{-\frac{t_{ij}}{\beta}}\right)^{\alpha_j}$$

The failure rate or hazard rate is given by

$$h(t_{ij}, \alpha_j, \lambda) = \frac{\frac{\alpha_j}{\beta} e^{-\frac{t_{ij}}{\beta}} \left(1 - e^{-\frac{t_{ij}}{\beta}}\right)^{\alpha_j - 1}}{1 - \left(1 - e^{-\frac{t_{ij}}{\beta}}\right)^{\alpha_j}}$$

One and only the shape boundary j decides the risk capability's shape. The summed up remarkable circulation has a log-curved thickness for $j = 1$ and a log-raised thickness for $j = 1$, as might be seen. The summed up remarkable circulation consequently displays a rising danger capability for $j = 1$ and a diminishing peril capability for $j = 1$ for the decent worth of scale boundary. It has a consistent peril capability for $j = 1$. As indicated by Ahmad (2010), the summed up dramatic dispersion's danger capability acts unequivocally equivalent to the gamma appropriation's risk capability, which is extensively not the same as the Weibull conveyance's peril capability.

Moreover, it is assumed that the stress $V_j, j = 1, 2, \dots, k$ just impacts the Summed up Dramatic Model's shape boundary, j , through a particular speed increase capability remembered to be a power rule model, which has the accompanying structure:

$$\alpha_j = CV_j^{-p}; \quad C > 0, p > 0, \quad j = 1, 2, \dots, k$$

where the parameters for this model are C , the proportionality constant, and p , the power of the applied stress.

THE ESTIMATION PROCEDURE

The greatest probability assessment technique is utilized in light of the fact that it is truly dependable and produces boundary gauges with positive measurable attributes. fostered the probability capability for a perception at feeling of anxiety V_j of the chance to disappointment. Since n_j units are tried at each feeling of anxiety, V_j . In this manner, $N = n_j$ addresses the general number of units utilized in the tests. The i th try closes after the editing time " t_0 " is accomplished when a sort I controlling is utilized at each feeling of anxiety. Accept that the test is suspended once r_j surrenders are found at the j th anxiety, yet $n - r_j$ units keep on working appropriately. The accompanying structure is remembered to address the probability capability of the trial.

$$L(\alpha_j, C, \beta) = \prod_{j=1}^k \frac{n_j}{(n_j - r_j)!} \left[\prod_{i=1}^{r_j} f(t_{ij}; \alpha_j, C, \beta) \right] \left[1 - F(t_0) \right]^{n_j - r_j}$$

where t_0 represents the moment the test was stopped.

The natural logarithm of L , C , and, denoted by $\ln L$, is given by

$$\ln L = K + \sum_{j=1}^k r_j (\ln C - \ln \beta) - p \sum_{j=1}^k r_j \ln V_j - \sum_{j=1}^k \sum_{i=1}^{r_j} \frac{t_{ij}}{\beta} + \sum_{j=1}^k \sum_{i=1}^{r_j} (CV_j^{-p} - 1) \ln(W(t_{ij})) + \sum_{j=1}^k (n_j - r_j) \ln \left[1 - (W(t_0))^{CV_j^{-p}} \right]$$

$$\text{where, } K \text{ is a constant, } W(t_{ij}) = 1 - \exp\left(-\frac{t_{ij}}{\beta}\right) \& W(t_0) = 1 - \exp\left(-\frac{t_0}{\beta}\right)$$

The probability function's logarithm's first derivative with regard to, C , and p is given by:

$$\frac{\partial \ln L}{\partial \beta} = -\sum_{j=1}^k \frac{r_j}{\beta} + \sum_{j=1}^k \sum_{i=1}^{r_j} \frac{t_{ij}}{\beta^2} - \sum_{j=1}^k \sum_{i=1}^{r_j} \frac{(CV_j^{-p} - 1) t_{ij}}{W(t_{ij}) \beta^2} \exp\left(\frac{-t_{ij}}{\beta}\right) + \sum_{j=1}^k \frac{(n_j - r_j) t_0 CV_j^{-p}}{\phi(t_0) \beta^2} (W(t_0))^{CV_j^{-p}-1} \exp\left(-\frac{t_0}{\beta}\right)$$

$$\frac{\partial \ln L}{\partial C} = \sum_{j=1}^k \frac{r_j}{C} + \sum_{j=1}^k \sum_{i=1}^{r_j} V_j^{-p} \ln W(t_{ij}) - \sum_{j=1}^k \frac{(n_j - r_j)}{\phi(t_0)} V_j^{-p} (W(t_0))^{CV_j^{-p}} \ln(W(t_0))$$

$$\frac{\partial \ln L}{\partial p} = \sum_{j=1}^k r_j \ln V_j - \sum_{j=1}^k \sum_{i=1}^{r_j} CV_j^{-p} \ln V_j \ln(W(t_{ij})) + \sum_{j=1}^k \frac{(n_j - r_j)}{\phi(t_0)} CV_j^{-p} \ln V_j \ln W(t_0) (W(t_0))^{CV_j^{-p}}$$

$$\text{Where, } \phi(t_0) = 1 - (W(t_0))^{CV_j^{-p}}$$

Likening conditions to nothing and settling them at the same time utilizing an iterative technique yields the greatest probability assessors of, C, and p. Also, by subbing expected values with their greatest probability assessors and transforming the fisher data lattice, which is characterized by:

$$I = \begin{bmatrix} -\frac{\partial^2 \ln L}{\partial \beta^2} & -\frac{\partial^2 \ln L}{\partial C \partial \beta} & -\frac{\partial^2 \ln L}{\partial p \partial \beta} \\ -\frac{\partial^2 \ln L}{\partial \beta \partial C} & -\frac{\partial^2 \ln L}{\partial C^2} & -\frac{\partial^2 \ln L}{\partial p \partial C} \\ -\frac{\partial^2 \ln L}{\partial \beta \partial p} & -\frac{\partial^2 \ln L}{\partial C \partial p} & -\frac{\partial^2 \ln L}{\partial p^2} \end{bmatrix}$$

The logarithm of probability function is defined in equation and its second derivatives are as follows:

$$\frac{\partial^2 \ln L}{\partial \beta^2} = \sum_{j=1}^k \frac{r_j}{\beta^2} - 2 \sum_{j=1}^k \sum_{i=1}^{r_j} \frac{t_{ij}}{\beta^3} - \sum_{j=1}^k \sum_{i=1}^{r_j} \left[(CV_j^{-p} - 1) t e^{\frac{t_{ij}}{\beta}} \frac{2\beta e^{\frac{t_{ij}}{\beta}} - 2\beta - t_{ij}}{\beta^4 (e^{\frac{t_{ij}}{\beta}} - 1)^2} \right] + \sum_{j=1}^k (n_j - r_j) t_0 CV_j^{-p} \left[\frac{(W(t_0))^{CV_j^{-p}} \left\{ (2V_j^p \beta^3 - t_0 V_j^p \beta^2) (W(t_0))^{CV_j^{-p}} + t_0 V_j^p \right\} e^{\frac{t_0}{\beta}} - 2V_j^p \beta^3 (W(t_0))^{CV_j^{-p}} - C t_0}{V_j^p \left\{ \beta^2 (W(t_0))^{CV_j^{-p}} - 1 \right\}^2 \left(e^{\frac{t_0}{\beta}} - 1 \right)^2} \right]$$

$$\frac{\partial^2 \ln L}{\partial C^2} = -\sum_{j=1}^k \frac{r_j}{C^2} - \sum_{j=1}^k (n_j - r_j) V_j^{-p} (W(t_0))^{CV_j^{-p}} \left\{ \ln(W(t_0)) \right\}^2 \left\{ \frac{\phi(t_0) V_j^{-p} + (W(t_0))^{CV_j^{-p}} V_j^{-p}}{(\phi(t_0))^2} \right\}$$

$$\begin{aligned} \frac{\partial^2 \ln L}{\partial p^2} &= \sum_{j=1}^k \sum_{i=1}^{r_j} C V_j^{-p} (\ln V_j)^2 \ln W(t_{ij}) + \\ &\quad \sum_{j=1}^k (n_j - r_j) \ln V_j C V_j^{-2p} \ln W(t_0) \left[\frac{(W(t_0))^{C V_j^{-p}} \ln V_j \{ \phi(t_0) V_j^{-p} + C \ln W(t_0) \}}{(\phi(t_0))^2} \right] \\ \frac{\partial^2 \ln L}{\partial \beta \partial C} &= - \sum_{j=1}^k \sum_{i=1}^{r_j} \frac{t_{ij}}{\beta^2} e^{-\frac{t_{ij}}{\beta}} + \sum_{j=1}^k (n_j - r_j) t_0 (W(t_0))^{C V_j^{-p}} \left[\frac{C \ln W(t_0) + V_j^p}{\phi(t_0) \beta^2 \left(e^{\frac{t_0}{\beta}} - 1 \right)} \right] \\ \frac{\partial^2 \ln L}{\partial p \partial C} &= - \sum_{j=1}^k \sum_{i=1}^{r_j} V_j^{-p} \ln W(t_{ij}) \ln V_j - \sum_{j=1}^k (n_j - r_j) \ln W(t_0) \left[(W(t_0))^{C V_j^{-p}} \left(\frac{C \ln W(t_0) - \phi(t_0)}{\phi(t_0) V_j^{2p}} \right) \right], \\ \frac{\partial^2 \ln L}{\partial \beta \partial p} &= \sum_{j=1}^k \sum_{i=1}^{r_j} \frac{t_{ij}}{\beta^2} \frac{\ln V_j}{W(t_{ij})} e^{-\frac{t_{ij}}{\beta}} + \sum_{j=1}^k t_0 \frac{(n_j - r_j)}{V_j^p \beta^2} C V_j^{-p} \ln V_j (W(t_0))^{C V_j^{-p}} \left[\frac{C \ln W(t_0) + V_j^p \phi(t_0)}{(\phi(t_0))^2 (e^{t_0/\beta} - 1)} \right] \end{aligned}$$

Therefore, the Fisher information matrix defined in above equation was inverted to produce an asymptotic variance-covariance matrix for the MLE of, C & p.

Therefore, the approximate 1-100-00 confidence intervals for C, p, and are as follows:

$$\hat{\beta} \pm Z_{\lambda/2} \sqrt{\text{var}(\hat{\beta})}, \hat{C} \pm Z_{\lambda/2} \sqrt{\text{var}(\hat{C})}, \hat{p} \pm Z_{\lambda/2} \sqrt{\text{var}(\hat{p})},$$

where $Z/2$ represents a standard normal variate's 100-1/2 percentile.

SIMULATION PROCEDURE

Unquestionably the relative predisposition (RABs) and mean square mistake (MSE) of the MLEs are concentrated on mathematically in this segment to analyze how well they perform. The MLEs of shape Boundary can be figured by the accompanying condition utilizing the invariance state of MLEs.

$$\alpha_j = C V_j^{-p}; \quad C > 0, p > 0, \quad j = 1, 2, \dots, k$$

Below are the specific steps.

- A generalised exponential distribution was used to create 1000 random samples of sizes 50, 100, 150, and 200. All sets of parameters are given different starting values.
- Because there are only three distinct stress levels, or $k=3$, the stress values are chosen as $V_1 = 1$, $V_2 = 1.5$, and $V_3 = 2$, with $n_j = n$ and $r_{3j} = 60\% n_j$.
- The model's parameters were calculated from type-I censored samples for all sample sizes.
- The Newton-Raphson method is used to solve all equations. Equation yields an approximation of the scale parameter j .
- The RABs and MSE for all sets of 0, C0, and p0 were tabulated.
- Calculate the MLEs of the shape parameter u at the typical stress level $V_u 0.5$ using the MLEs' invariance characteristic. Calculate the reliability function for various values of ,C, p & t_0 , with the same normal stress.

$$\hat{R}_u(t_0) = 1 - \left(1 - e^{-\frac{t}{\beta_0}} \right)^{\alpha_0}$$

Furthermore, given the same typical circumstance for all sets of parameters, the MLEs of the reliability function at mission time t_0 are projected.

Tables (1.1), (1.2), and (1.3) provide summaries of the simulation results. The estimators, RABs, and MSEs are shown in Tables (1.1) and (1.2). The dependability function is predicted under $V_u 0.5$ in Tables (1.3), and the anticipated form parameter is given under $V_u 0.5$.

Table 1.1
The Estimates, Relative Bias and MSE of the parameters
($\beta, C, P, \alpha_1, \alpha_2, \alpha_3$) under type-II censoring

| n | parameters | $(\beta_0=0.25, C_0=1.5, p_0=1)$ | | | $(\beta_0=1, C_0=1.5, p_0=1)$ | | |
|-----|------------|----------------------------------|-------|-------|-------------------------------|-------|-------|
| | | Estimator | RABs | MSEs | Estimator | RABs | MSEs |
| 50 | β | 0.229 | 0.084 | 0.078 | 0.930 | 0.070 | 0.076 |
| | C | 1.411 | 0.059 | 0.044 | 1.421 | 0.052 | 0.063 |
| | P | 0.930 | 0.070 | 0.062 | 0.925 | 0.075 | 0.071 |
| | α_1 | 1.411 | 0.059 | 0.044 | 1.421 | 0.052 | 0.063 |
| | α_2 | 0.967 | 0.057 | 0.042 | 0.976 | 0.050 | 0.062 |
| | α_3 | 0.740 | 0.056 | 0.042 | 0.748 | 0.049 | 0.059 |
| 100 | β | 0.234 | 0.064 | 0.064 | 0.947 | 0.053 | 0.056 |
| | C | 1.429 | 0.047 | 0.035 | 1.436 | 0.042 | 0.048 |
| | P | 0.933 | 0.067 | 0.071 | 1.098 | 0.098 | 0.077 |
| | α_1 | 1.429 | 0.047 | 0.035 | 1.436 | 0.042 | 0.048 |
| | α_2 | 0.955 | 0.045 | 0.034 | 0.920 | 0.040 | 0.046 |
| | α_3 | 0.748 | 0.044 | 0.033 | 0.670 | 0.039 | 0.045 |
| 150 | β | 0.239 | 0.044 | 0.042 | 0.951 | 0.049 | 0.051 |
| | C | 1.449 | 0.034 | 0.034 | 1.561 | 0.040 | 0.041 |
| | P | 0.946 | 0.054 | 0.046 | 1.052 | 0.052 | 0.046 |
| | α_1 | 1.449 | 0.034 | 0.034 | 1.561 | 0.040 | 0.041 |
| | α_2 | 0.987 | 0.033 | 0.033 | 1.018 | 0.039 | 0.040 |
| | α_3 | 0.752 | 0.032 | 0.032 | 0.752 | 0.038 | 0.039 |
| 200 | β | 0.252 | 0.008 | 0.010 | 0.976 | 0.024 | 0.030 |
| | C | 1.480 | 0.013 | 0.003 | 1.467 | 0.022 | 0.023 |
| | P | 1.113 | 0.113 | 0.010 | 0.955 | 0.045 | 0.031 |
| | α_1 | 1.480 | 0.013 | 0.003 | 1.467 | 0.022 | 0.023 |
| | α_2 | 0.942 | 0.012 | 0.002 | 0.996 | 0.021 | 0.023 |
| | α_3 | 0.684 | 0.012 | 0.003 | 0.756 | 0.021 | 0.022 |

Table 1.2
The Estimates, Relative Bias and MSE of the parameters
($\beta, C, P, \alpha_1, \alpha_2, \alpha_3$) under type-II censoring

| n | parameters | $(\beta_0=0.25, C_0=1, p_0=1)$ | | | $(\beta_0=1, C_0=1, p_0=1.5)$ | | |
|----|------------|--------------------------------|-------|-------|-------------------------------|-------|-------|
| | | Estimator | RABs | MSEs | Estimator | RABs | MSEs |
| 50 | β | 0.231 | 0.076 | 0.081 | 0.928 | 0.072 | 0.067 |
| | C | 1.103 | 0.103 | 0.047 | 1.071 | 0.071 | 0.067 |
| | P | 0.929 | 0.071 | 0.058 | 1.421 | 0.052 | 0.063 |
| | α_1 | 1.103 | 0.103 | 0.047 | 1.071 | 0.071 | 0.067 |
| | α_2 | 0.756 | 0.074 | 0.046 | 0.601 | 0.069 | 0.065 |
| | α_3 | 0.579 | 0.072 | 0.045 | 0.400 | 0.068 | 0.064 |

| | | | | | | | |
|-----|------------|-------|-------|-------|-------|-------|-------|
| 100 | β | 0.237 | 0.052 | 0.057 | 0.939 | 0.061 | 0.055 |
| | C | 1.098 | 0.098 | 0.042 | 1.056 | 0.044 | 0.050 |
| | P | 0.937 | 0.063 | 0.075 | 1.436 | 0.042 | 0.065 |
| | α_1 | 1.098 | 0.098 | 0.042 | 1.056 | 0.044 | 0.050 |
| | α_2 | 0.750 | 0.095 | 0.040 | 0.590 | 0.043 | 0.049 |
| | α_3 | 0.573 | 0.093 | 0.039 | 0.390 | 0.043 | 0.048 |
| 150 | β | 0.239 | 0.044 | 0.045 | 0.948 | 0.052 | 0.042 |
| | C | 1.049 | 0.049 | 0.033 | 1.041 | 0.041 | 0.036 |
| | P | 0.958 | 0.042 | 0.040 | 1.561 | 0.040 | 0.056 |
| | α_1 | 1.049 | 0.049 | 0.033 | 1.041 | 0.041 | 0.036 |
| | α_2 | 0.711 | 0.048 | 0.032 | 0.552 | 0.040 | 0.035 |
| | α_3 | 0.539 | 0.047 | 0.032 | 0.352 | 0.039 | 0.034 |
| 200 | β | 0.252 | 0.008 | 0.017 | 0.981 | 0.019 | 0.036 |
| | C | 1.060 | 0.060 | 0.023 | 1.035 | 0.025 | 0.031 |
| | P | 1.013 | 0.013 | 0.021 | 1.467 | 0.022 | 0.025 |
| | α_1 | 1.060 | 0.060 | 0.023 | 1.035 | 0.025 | 0.031 |
| | α_2 | 0.702 | 0.060 | 0.022 | 0.570 | 0.024 | 0.030 |
| | α_3 | 0.525 | 0.059 | 0.022 | 0.374 | 0.024 | 0.030 |

Table 1.3

The estimated shape parameter and Reliability function at normal stress level taking n=200.

| β_0 | C_0 | P_0 | α_0 | t_0 | $R_U(t_0)$ |
|-----------|-------|-------|------------|-------|------------|
| 0.25 | 1.5 | 1 | 3.201165 | 0.2 | 0.8518 |
| | | | | 0.4 | 0.5141 |
| | | | | 0.6 | 0.2624 |
| 1 | 1.5 | 1 | 2.843896 | 0.2 | 0.9922 |
| | | | | 0.4 | 0.9573 |
| | | | | 0.6 | 0.8959 |
| 0.25 | 1 | 1 | 2.139189 | 0.2 | 0.7208 |
| | | | | 0.4 | 0.3826 |
| | | | | 0.6 | 0.1840 |
| 1 | 1 | 1.5 | 2.861221 | 0.2 | 0.9924 |
| | | | | 0.4 | 0.9581 |
| | | | | 0.6 | 0.8974 |

THE AGERE PLACEMENT POLICY UNDERPRO-RATAREBATE WARRANTY

A non-repairable item will be supplanted under this guarantee at a particular age (t_0) or upon disappointment, whichever starts things out. At the point when an item glitches at time t , a disappointment supplanting is done with no free time cost and no buy cost. A piece of the price tag (C_p) is gotten back to the buyer on the off chance that the item breakdowns inside the guarantee period (w). The supportive of rata guarantee's discount include is: There is some writing on age-substitution strategy. Taking into account an age-supplanting model with least fix in light of a total fix cost cap and an irregular lead time for substitution conveyance, (Chien and Chen, 2007a) proposed. The effects of a reestablishing free-substitution guarantee (RFRW) on the age trade strategy for a repairable item with an overall disappointment model were again inspected by Chen and Chen (2007b). Huang et al. (2008) took a gander at the issue of working out the normal guarantee cost for the circumstance where the thing utilization is inconsistent and of variable power throughout the item life cycle when deals happen continually. They considered items that could be fixed and those that proved unable, and they found solutions for

the free-substitution guarantee (FRW) and supportive of rata guarantee (PRW) arrangements. The effects of rescue esteem on the ideal age-substitution methodology for non-repairable gadgets sold with an expert rata refund guarantee (PRRW) were examined by Chien (2010). The effects of rescue esteem on the ideal age-trade strategy for non-repairable gadgets sold with a recharging free-substitution guarantee (RFRW) were examined by Chien et al. (2014). Na and Sheng (2014) explored the impact of guarantee spans on the best age-substitution from the outlook of the buyer. The numerical details for the age-substitution model were first fabricated. The objective of the ongoing review was to appraise the in general expected cost and the extended expense rate for age substitution of units covered by guarantee. The expected all out cost and expected cost rate for age substitution under the favorable to rata discount guarantee strategy are additionally included.

THE MAIN ASSUMPTIONS:

- Contingent upon which happens first, either the item is supplanted at the weak spot (restorative substitution) or as it ages (preventive substitution).
- A supportive of rata discount guarantee is incorporated with the offer of the item.
- The item that was supplanted as a protection measure has no rescue esteem.
- The guarantee time frame (w) is more limited than the age substitution (τ).

Since it is an arranged preventive support activity, the protection substitution is possibly completed when the item age surpasses.

The whole cost for this approach's restoration cycle is:

$$C(d) = \begin{cases} Cd + Cp - R(t) & 0 \leq t \leq w \\ Cd + Cp & w < t < \tau \\ Cp & t \geq \tau \end{cases}$$

The projected total cost under this policy, as stated by Chein (2010) and Chein et al. (2014), is provided by:

$$E(C(t)) = CdF(\tau) + Cp \frac{\int_0^w \bar{F}(u) du}{w}$$

The anticipated cost rate is also

$$E(CR(t)) = \frac{E(C(t))}{\int_0^{\tau} \bar{F}(u) du}$$

Where E.T. stands for expected cycle time, which is represented by $\int_0^{\tau} \bar{F}(u) du$.

UNDER GENERALISED EXPONENTIAL DISTRIBUTION:

A CDF is provided by

$$F(u) = \left(1 - e^{-\frac{u}{\beta}}\right)^{\alpha}; u > 0, \alpha, \beta > 0$$

Therefore

$$\int_0^w \bar{F}(u) du = w - \int_0^w \left(1 - e^{-\frac{u}{\beta}}\right)^\alpha du$$

$$\text{Also, } \int_0^\tau \bar{F}(u) du = \tau - \int_0^\tau \left(1 - e^{-\frac{u}{\beta}}\right)^\alpha du$$

Conditions are individually subbed into conditions to deliver the extended complete expense and anticipated cost rate for the non-repairable item. Obviously the capability depicted by the previously mentioned conditions comes up short on crucial basic. Subsequently, by subbing the upsides of the multitude of important elements, barring the variable of mix, a mathematical guess can be inferred.

As a delineation, assume the disappointment supplanting is done with a margin time cost of Cd of 50 and a buy cost of Cp of 1000. Gauges are made of the expected absolute expense, expected cycle length, and expected cost rate for age-trade under guarantee strategy for different guarantee period values (w) and summed up dramatic dispersion boundaries (and) under ordinary use.

Table 1.4

The expected total cost, the expected cycle time and the expected cost rate forage-replacement under warranty policy on Generalized Exponential distribution.

| β | α | w | τ | E(C(τ)) | E(T(τ)) | CR(τ) |
|---------|----------|---|--------|----------------|----------------|--------------|
| 2 | 0.2 | 5 | 7 | 930.1232 | 5.7921 | 230.885 |
| 3 | 0.2 | 5 | 7 | 944.1763 | 6.4909 | 215.4057 |
| 4 | 0.2 | 5 | 7 | 955.8282 | 6.9264 | 199.7983 |
| 5 | 0.2 | 5 | 7 | 973.2882 | 7.3589 | 174.5714 |
| 5 | 0.3 | 5 | 7 | 882.6932 | 6.0825 | 183.0282 |
| 5 | 0.4 | 5 | 7 | 830.1848 | 5.2488 | 204.6751 |
| 5 | 0.4 | 6 | 7 | 903.7913 | 6.2867 | 208.0381 |
| 5 | 0.4 | 7 | 7 | 947.5114 | 7.5112 | 218.3333 |
| 5 | 0.4 | 8 | 8 | 988.8976 | 8.0751 | 203.3333 |
| 5 | 0.4 | 8 | 9 | 1012.512 | 8.4758 | 200.4356 |
| 5 | 0.4 | 8 | 10 | 1050.812 | 8.8752 | 216.6667 |

CONCLUSION:

These assessors are alluded to as steady assessors since it very well may be normal from tables (1.1) and (1.2) that the outright worth of the distinction between the boundary's actual worth and its assessor is unobtrusive positive worth unites to nothing. The reliability capability is assessed in table (1.3) at different mission time t0 and 0 qualities. Seen that as mission time t0 develops, the dependability capability brings down too. It's a given that in the event that an item is tried for quite a while, its dependability diminishes because of item wear.

The accompanying discoveries are found in table (1.4).

- The worth of the boundary and the expected absolute expense and time cycle have an opposite association.
- The anticipated expense rate and the boundary's worth have an immediate connection.
- The worth of boundary has a converse connect to anticipated cost rate and an immediate relationship to expected time cycle and all out cost.
- Broadening the guarantee term prompts the extended all out cost and the normal expense rate to increase, yet it no affects the expected life cycle.
- While there are immediate connections with the normal complete expense and projected time cycle, there is a converse connection between the period of substitution and the assessed cost rate.

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